

Lösung Kap 3 incl DB 4

1 a)

$$\left(\frac{2m-3n}{3r} - \frac{m+4n}{2t} \right) : \left(\frac{4t-3r}{6n} - \frac{t+2r}{m} \right)$$

$$\frac{4mt - 6nt - 3mr - 12nr}{6rt} \cdot \frac{6mn}{4mt - 3mr - 6nt - 12nr} = \underline{\underline{\frac{mn}{rt}}} \quad (2)$$

6)

$$\frac{5n-15m}{105abc} \cdot \frac{3x+6y}{6a} \cdot \frac{84ab}{nx+2ny-3mx-6my} =$$

$$\frac{\cancel{5}^1(n-3m)}{\cancel{105}^7 \cdot \cancel{abc}^1} \cdot \frac{\cancel{3}^1(x+2y)}{\cancel{6}^2 a} \cdot \frac{\cancel{84}^7 ab}{\cancel{nx+2ny-3mx-6my}^2}$$

$$\frac{(n-3m)(x+2y) \cdot 2}{ac(n-3m)(x+2y)} = \underline{\underline{\frac{2}{ac}}} \quad (3)$$

2

$$\left(\frac{7a-5n}{4b} - \frac{27nx}{4b} + \frac{7ab}{6x} - \frac{6n}{2x} \right) : \left(\frac{9}{8b} + \frac{2}{6x} \right) =$$

$$\left(\frac{63ax - 27nx}{4b} + \frac{7ab - 3bn}{6x} \right) : \left(\frac{27x^2 + 2b^2}{3bx} \right) =$$

$$\frac{189ax^2 - 81nx^2 + 7ab^2 - 6b^2n}{4bx} \cdot \frac{3bx}{27x^2 + 2b^2} =$$

$$\frac{27x^2(7a-5n) + 2b^2(7a-3n)}{4(27x^2 + 2b^2)} = \frac{(27x^2 + 2b^2)(7a-3n)}{4(27x^2 + 2b^2)}$$

$$= \underline{\underline{\frac{7a-3n}{4}}}$$

$$3 \ a) \quad \frac{\overset{(a-b)}{a}}{a+b} + \frac{\overset{(a+b)}{b}}{a-b} = \frac{a^2 - \cancel{ab} + \cancel{ab} + b^2}{a^2 - b^2} = \frac{a^2 + b^2}{a^2 - b^2}$$

$\frac{\cancel{a-b}}{\cancel{a-b}} = (1)$

$$b) \quad \frac{1}{x + \frac{1}{x + \frac{1}{x+1}}} = \frac{1}{x + \frac{1}{\frac{x^2+x+1}{x+1}}} = \frac{1}{x + \frac{x+1}{x^2+x+1}}$$

$$= \frac{1}{\frac{x(x^2+x+1) + x+1}{x^2+x+1}} = \frac{x^3 + x^2 + x + x + 1}{x^2+x+1}$$

$$= \frac{x^2 + x + 1}{x^3 + x^2 + 2x + 1}$$

$$4 \quad \left(\frac{56}{3} - \frac{175mnxy}{36acd} + \frac{12abcd}{5xy} - 7mn \right) : \left(\frac{3ab}{5xy} - \frac{7mn}{4cd} \right)$$

$\frac{300abcdxy - 875mnx^2y^2 + 432a^2b^2c^2d^2 - 1260acdmnxy}{180acdxy}$

$$\cdot \left(\frac{12abcd - 35mnxy}{20cdxy} \right) =$$

$$\frac{(12abcd(25xy + 36acd) - 35mnxy(25xy + 36acd))}{180acdxy} \cdot \frac{1}{20cdxy} = \frac{(25xy + 36acd)(12abcd - 35mnxy)}{180acdxy \cdot 20cdxy} = \frac{25xy + 36acd}{9}$$

oder $\frac{25xy}{9} + 4acd$